

## Similar Matrices

Let  $A$  and  $B$  be square matrices of order  $n$ . Then  $B$  is said to be similar to  $A$  if there exists a non-singular matrix  $P$  such that

$$B = P^{-1}AP$$

### Properties

\* A matrix ~~A~~ is similar to itself

\* If  $A$  is similar to  $B \Rightarrow B$  is similar to  $A$ .

\* Equivalence relation:

$A$  is similar to  $B$ ,  $B$  is similar to  $C \Rightarrow A$  is similar to  $C$

\* If  $A$  is similar to  $B$

$$\Rightarrow \text{determinant } A = \text{determinant } B$$

$$\text{i.e. } |A| = |B|$$

\*  $A$  is similar to  $B \Rightarrow \text{trace } A = \text{trace } B$ .

\*  $A$  is similar to  $B \Rightarrow A^m$  is similar to  $B^m$ ,  $m \in \mathbb{I}$

\* If  $A$  is similar to  $B$  then  $A$  is invertible

iff  $B$  is invertible.

Then  $A^{-1}$  is similar to  $B^{-1}$ .